Tailing the Hedge
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Example:

We sell a $100 forward on asset $S$ to a costumer and we want to hedge our risk. Suppose that there exists an exchange traded contract on futures of $S$ (trading also at $100$) and we want to hedge with that. How do we do this?
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We should have bought $e^{-rT}$ futures.